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ROUTING OF RETAIL PRODUCT DELIVERY IN URBAN ROAD SYSTEM ON THE BASIS OF GENETIC ALGORITHM

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A model simulating dynamic processes in a urban road system has been developed. On the basis of genetic search the methods of service route construction was created. System of automated transport routing delivering different goods was designed.

Introduction

In modern conditions of market economy the competitive advantage over the other participants of a certain market sector is a symbol of stable and successful development of any enterprise. Beneficial terms of manufacturing may be achieved due to wide spectrum of action. Qualitative organization of production distribution process is the competitive advantage for the enterprise. The main optimization directions are: operative preparation of applications and stable execution of orders in full volume and range. For this purpose the optimized traffic plan is required. The routs should meet a number of specific requirements:

- automobiles used in delivery have limited carrying capacity;
- limited number of automobiles defines the possibility of their repeated use;
- each route starts and finishes at finished-products storage area;
- clients automobile distribution and sequence of their route should minimize delivery costs;
- routs should reflect road situation changing during the day and conform to existing rule of the road.

Vehicle Routing Problem (VRP) is widely discussed in literature. The first investigations on this problem had already appeared at the beginning of the 70's of the last century [1, 2]. At present, not unsuccessful attempts are realized for solving this problem and its expansions both by exact and approximate methods. The majority of techniques existing up today solve the statistic variant of VRP. This situation is simplified and not always adequate to real conditions. For urban road systems (URS) the inconstancy of carrying capacity at many movement sections during the day are typical that influences inevitably on quality of work of various delivery services. Besides, almost each real URS abounds in one-way movement streets with constantly or occasionally illegal turns. The route overcoming time may also significantly depend on its configuration, as broken bypass schemes decrease the average rate of motion. The problem is especially urgent for retail food stores, where regular deliveries of relatively small consignments of goods are required. To construct storage rooms in such conditions is usually meaningless: the sold production has mostly very limited use-by date; additional areas involve additional costs for their maintenance.

VRP peculiarity at any graph is in the fact that the total rout, traversed by all used traffic, the time of all orders execution are influenced both by quality of many clients rout distribution and the quality of found route cycles of all clients by traffic units. This peculiarity is rather important at modeling networks with high inconstancy of carrying capacity that is typical for modern cities.

In the given paper the stated peculiarity of VRP is taken into consideration. The suggested technique for solution of routing problem consists of several stages: conversion of initial URS graph to the graph of a certain type, applying a specially modificated Deicstra algorithm; routs construction by means of developed metaheuristics on the basis of genetic algorithm (GA). The package permitting for efficient traffic plans, minimizing delivery costs is suggested as a part of GA. The choice of the method is justified by the fact that routing problem is NP complex, i. e. the size of search space has an exponential dependence on variables amount. In suggested extension it has very large and complex decision space even at relatively small quantity of clients. There is a number of sources, for example, [3], where the effectiveness of metaheuristics, especially GA, application for graph problems is shown in tests. And, the quality of solutions obtained in GA increases at growth of problem dimension in comparison with other methods.

Problem on construction of delivery plan for retail client network

Dynamic graph which simulates changes of streets carrying capacity, existence of one-way movement sections, constantly and occasionally illegal turns, increase of rout overcoming time, using more gradient turns connected with necessity to brake and to race again is used as the URS model. In the conditions of the dynamic graph the target criterion is an extent and duration balance of required routes.

Let us represent the urban road system in the form of directed bound graph $G = \langle D, U \rangle$, where $D = \{1, 2...n_D\}$ is the set of graph nodes with n_D power, U is the set of arcs connecting nodes. Graph junctions are considered to be both various points of production selling, for example, stores, dining halls, hospitals and kindergartens, and common crossings of highways. Let us distinguish a target subset of nodes $\hat{P} = \{1, 2...\hat{n}\}, \hat{P} \subset D$, which consists only of service customers. In Fig. 1 vertex set *D* is all graph nodes, *P* is the black nodes, $u_{ij} \in U$, $i, j \in D$ are the arcs between any adjacent nodes, and $u_{i,j} \neq u_{j,i}$. The finished-product storage area is labeled in left upper corner.

An enterprise manufactures production cyclically. Therefore, the whole set of clients \hat{P} , are distributed per production cycles when applications being received. Then, our task is to plan delivery for clients of a certain production cycle. $P \subset \hat{P}$ is taken as clients subset of a certain production cycle. Then, *n* is the number of clients, corresponding to a certain cycle, which should be served.



Fig. 1. Graph G is the model of urban road system

Streets carrying capacity is the time function and changes almost cyclically every day. Therefore, let us divide the whole daily range into *T* segments, inside of which the index is constant. Then, each arc $u_{i,j} \in U$ of graph *G* connecting nodes $i, j \in D$ and representing a certain section of a street possesses the extent $l(u_{i,j})$, km and average rate $w(u_{i,j}, \tau), \tau=1...T$, km/h at the moment τ , where τ is the discrete time determining a number of daily range. The number of range t is determined as time function $\tau=\tau(t)$, where t is the current simulated time.

q vehicles are at the disposal of shipping department. Each vehicle is characterized by lift capacity *K*, kg (m cube). The order of *I* client has the form: $d_i=(d_{iv}), i \in P$, $v \in S$, where d_{iv} is the volume *d* of product *v*, which should be delivered to the client *i*, *S* is the set of production manufactured at the enterprise.

The set of clients *P* should be broken down per vehicles so that total orders volume of the subset of clients assigned to a concrete vehicle for transportation does not increase this vehicle lift capacity. Let us denote set partition *P* into disjoint subsets by $p_1 \cup ... \cup p_k$ $\dots \cup p_a$, so that $p_k \cap p_s = \emptyset$, where α is the total amount of runs, *Y* is the set of all admissible set partitions *P*. For example, there is $p_1 = \{h, f, j, i\}, p_2 = \{e\}$ in Fig. 1. Then, loading of vehicles for products transportation to assigned customers is determined by inequality

$$\sum_{i\in p_k} d_i \le K_k, \ k = 1...\alpha.$$
(1)

It is necessary to calculate an optimal route of nodes of the assigned subset p_k of partition y for every used vehicle. Let us denote by permutation $z_k = (i_1...i_m...i_{g_{k-1}}, i_{g_k})$ the alternative order of nodes $i_m \in p_k$, $m=1...g_k$ route by vehicle k from set of all possible permutations Z_k . Here i_1 is the starting node, denoting route beginning, i. e. the finished-products storage area; $g_k - 1 = |p_k|$ is the amount of target nodes at the route. It is $z_1 = (i_1, h, i_j, j, f, i_k)$ in Fig. 1. The completion of route is in starting node, i. e. $i_{g_k} = i_1$. The routes should cover the nodes of sets p_k in order, providing minimal total delivery cost.

The main factors determining its cost are duration and length of routes. Therefore, their linear combination per each traffic unit is considered as target criteria that results in optimal use of traffic resources and, as a result, costs optimization. The target function is of the following form:

$$\sum_{k=1,\alpha} \left[\lambda l(z_k) + (1 - \lambda) \theta(z_k) \right] \to \min,$$
 (2)

where $l(z_k)$ and $\theta(z_k)$ are the length and duration of the route z_k respectively, λ is the weighting coefficient.

The length $l(z_k)$ of the route z_k is made up of paths lengths $\tilde{u}_{i_m,i_{m+1}}(\tau) \in U(\tau)$ connecting the nodes following one after another i_m , $i_{m+1} \in p_k$, $m=1...(g_k-1)$. There is $\tilde{u}_{i_m,i_{m+1}}(\tau)=(i,1,2,3,4,5,j)$ in Fig. 1. The path $\tilde{u}_{i_m,i_{m+1}}(\tau)$ is the function of discrete time τ , as the optimal route, connecting nodes i_m , i_{m+1} may considerably change in the course of the day, $\tau=\tau(t_{i_{m-1}})$, where $t_{i_{m-1}}$ is the departure time from the node i_{m-1} . The algorithm of set construction is described more detailed below.

The duration $\theta(z_k)$ of the route z_k is determined in the following way.

Let the time from current node i_m be calculated by the formula

$$t_{i_m} = \begin{cases} t_{i_m}^{\partial o} + t_{i_m}^{paix} \mid m = 2...g_k \\ t_k^{cmapm} \mid m = 1 \end{cases},$$
(3)

where $t_{i_m}^{\partial s}$ is the arrival moment into the node i_m from the node i_{m-1} ; t_k^{cmapm} is the vehicle k departure time from the storage are; $t_{i_m}^{pare}$ is the time interval, necessary for unloading client order $i_m \in p_k$, $k=1...\alpha$.

The magnitude $t_{i_m}^{\partial \theta}$ is made up of departure time from the previous node $t_{i_{m-1}}$ and the time for covering the distance $w(\tilde{u}_{i_m,i_{m+1}}(\tau))$ at average rate $l(\tilde{u}_{i_m,i_{m+1}}(\tau))$, $\tau = \tau(t_{i_{m-1}})$, returns the number of daily interval, corresponding to the current value $t_{i_{m-1}}$.

$$t_{i_m}^{\partial_{\theta}} = t_{i_{m-1}} + \frac{l(\tilde{u}_{i_{m-1},i_m}(\tau))}{w(\tilde{u}_{i_{m-1},i_m}(\tau))} , \quad i_m \in p_k .$$
(4)

The time of unloading order $t_{i_m}^{pase}$ is determined by the formula

$$t_{i_m}^{p_{a32}} = \tilde{t} \cdot \sum_{v \in S} d_{i_m, v} \quad , \quad i_m \in p_k \; , \tag{5}$$

where \tilde{t} is the average quantity of time for unloading 1 unit of product.

Then the time of the whole route of a single vehicle $\theta(z_k)$ equals the magnitude $t_{i_{k_k}}^{\partial e}$, defining the recurrence time of the vehicle k to the storage – node i_{e_k}

$$t_{i_{g_k}}^{\partial e} = t_{i_{g_{k-1}}} + \frac{l(\tilde{u}_{i_{g_{k-1}}, i_{g_k}}(\tau))}{w(\tilde{u}_{i_{g_{k-1}}, i_{g_k}}(\tau))}, \tau = \tau(t_{i_{g_{k-1}}}), i_{g_k} \in p_k , k = 1...\alpha.$$

Method of solution

URS together with retail chain may number more than a thousand points. Therefore, a large quantity of variants of clients coherence is possible. Let us divide the task of delivery routes organization into two main stages: simplification of initial graph of the urban road area (construction of reduced search space); direct routes finding.

Simplification of initial graph of the urban road area

To solve VRP in the stated statement let us construct a new graph $\tilde{G} = \langle \hat{P}, \tilde{U}(\tau) \rangle$, $\hat{P} \subset D$, $\tau = 1...T$ on the basis of the initial one G, where \hat{P} is the set of all clients, $\tilde{U}(\tau)$ is the set of paths, connecting clients in an optimal way for the daily interval τ .

To construct the set of arcs $\hat{U}(\tau)$, $\tau=1...T$ let us apply the Deicstra algorithm [4], which is specially modified for these purposes. The algorithm includes in modified form: the length $l(u_{i,j})$, $u_{i,j} \in U$, $i,j \in \hat{P}$ of initial arcs, the average speed $w(u_{i,j},t)$ in the current interval, forbidden turns for the moment τ , one-way movement roads, as well as fine taking for turns of high gradient. The algorithm operates during linear time.

Applying the algorithm $\hat{n}(\hat{n}-1)T$ times we construct the simplified graph for each τ . As a result, the sets combination $\tilde{U}(\tau)$, $\tau=1...T$ forms fully acceptable, optimally reduced search space, including URS specific character, where it is clear at every moment of the time, what route should be followed from one target node to another.

The finished graph G may be stored in a separate data base and recalculated only at change of constant clients list – appearance of new ones or deletion of passive clients during the specified time.

Routes finding. Solution of routing problem of traffic units for clients' service is realized in the form of GA.

Genetic algorithm architecture

Genetic algorithm represents the random search technique [5, 6].

The profile of solutions is selected for a specific type of investigated problem and should provide an adequate presentation of any point of decision space. Let us consider the sequence of serviced clients, in which the delivery of products is fulfilled as an alternative solution. For example, the first alternative in solution population of the form

$$p_{1}:1-2-5-11-7-4-6$$

$$p_{2}:6-11-7-5-2-1-4$$

$$\dots$$

$$p_{n}:6-7-4-2-11-1-5$$
(6)

indicates the fact that if the first vehicle is loaded only with the first three clients, not violating the condition (1), then its route will be as follows: 0-1-2-5-0, if there is room for all the rest clients in the next vehicle, then its route will be as follows: 0-11-7-4-6-0, where zero is the finished-products storage area.

For starting the search process it is necessary to create start population of solution-chromosomes. In our case, the mixed network of initialization is applied. A part of population is created with the help of well known the method of the Nearest Neighbour [7]. Creating the rest of individuals the generator of random numbers giving acceptable sequences at the finite set of clients P is used. The given network allows improving significantly the search at marked clients' clasterity.

Fitness of alternative chromosomes (quality of solutions) is estimated by specially developed heuristic function, easily realized in any program language. Functional diagram of the algorithm is represented in Fig. 2.



Fig. 2. Functional diagram of estimation algorithm

- 1. The cycle of alternatives estimation, where *m* is the size of population.
- 2. The cycle of available traffic search.
- 3. Set of time for start of delivery carrying out for connecting with concrete time interval τ .
- 4. The cycle of loading clients orders *j* into the current vehicle in the order, determined by the current chromosome.
- 5. Check-out of the place in the vehicle *k* for loading the order of client *j*.
- 6. Loading of the next order.

When loading the order, the available in the vehicle place for the size, corresponding to the order, is corrected. In this case, the meters of traversed path and time spent for the way and order unloading increase by values of corresponding arcs characteristics $\tilde{u}(\tau)$ connecting clients neighbour in solution (3, 4). We also take into consideration the arcs connecting the first and the last client with the storage area. The correction of current time *t* at the end of unloading results in change, if the current time overruns the interval. It allows selecting the optimal route to the next client.

The potential amount of orders, which can be loaded, depends on their volume; therefore, the amount of nodes in one vehicle may vary over a wide range. Therefore, the system of solution, coding not traffic units with the lists of serviced clients, but their simple sequence was suggested. That allows, in conjunction with the described estimation algorithm, using efficiently the dedicated storage having simplified as much as possible the structure of coded solutions (6) and excepting a single monitor unit of acceptability of alternatives obtained during evolution. The infeasible solutions, from the point of view of traffic overloading, are excluded.

At every estimation the capacities of available vehicles are imposed to the alternative sequence of clients in strictly fixed order for the whole evolution, that is the strictly consequence dynamic traffic loading by clients is performed. Therefore, within the evolutionary process, those alternatives where comparatively close clients are grouped according to the vehicles capacities and in the sequence, providing minimum of target function, become the best solutions (1).

The combination of solution representation system and estimation technique in the give GA possesses the key properties for the problem: in evolutionary process the parallel search of nodes optimal partition by the routes and optimal order of clients' route inside each set occur.

Here the selection policy of parents by the principle of roulette wheel and elite strategy is used. Thus, the loss of good solutions at application of genetic operators is excluded. Using genetic operators the creation of new individuals not presenting in population before is performed. Scanning search space is performed by operators of crossing, mutation, inversion. The corresponding operator of crossing is partially applied. The choice is made due to such problem situation that any client may be served only once by one vehicle: $p_k \cap p_s = \emptyset$, $k \neq s$, $k, s = 1...\alpha$. That is, the descendant should have the same gene structure that the initial individuals. The modifications appear only in the order of nodes sequence. Application of mean mutation – local searching strategies modifying the original solution on the basis of target function analysis or some of its parameters allows increasing significantly the quality of solutions. The description of local searching methods and various genetic operators is widely represented in literature and Internet, for example, in [5, 6].

Conditions of search stop:

- algorithm performed the given quantity of iterations *AbsN*;
- during *LocN* iterations the best solution is not changed.

Comparative results and approach efficiency

Trail calculations for static test problems published in scientific literature and available in Internet show good results comparable with best achievements published

REFERENCES

- Christofides N., Eilon S. An algorithm for the vehicle-dispatching problem // Operational Research Quarterly. – 1969. – № 20. – Р. 309–318.
- Christofides N., Mingozzi A., Toth P. The vehicle routing problem. In: Christofides N, Mingozzi A, Toth P. Sandi C., editors. Combinatorial optimization. – London: Wiley, 1979.
- Minakov I.A. Comparative analysis of some methods of random search and optimization // The Bulletin of RAS SC, Samara. 1999.
 № 2. P. 286–293.

in literature [8]. In many problems deviations achieve less than 2 %. There are no standard problems on the dynamic graphs. It should be mentioned that the quality of solutions including their stability depends essentially on the time set for searching. For example, for the problem with 200 clients, at *LocN*=200, the average search time is 40 s, and scatter of readings may reach 5...7 % from the best solution searched by algorithm. At *LocN*=2000 the average search time already equals 7 min, and the scatter of readings is 2...3 %.

The approach suggested above implies such search strategy that the routes found on the dynamic graph provide the best results at their use in real conditions in comparison with the results found on the static graph. The following estimation technique of searching efficiency in the dynamic graph was suggested. Let P_1 be the solution of the problem found on the static graph, P_2 is the same on the dynamic graph. Let us denote the quality of the solution determined by the weights of the static graph by L(P), where P is a certain solution. The estimation of solution Pin the dynamic graph is H(P). Let us take $L(P_1)$ as a lower estimate, as the solution is found in easy road conditions. Probably, $H(P_1)$ is the worst estimation, since the solution P_1 does not include the peculiarities of the dynamic graph. The simulation error is denoted by $\Delta_1 = H(P_1) - L(P_1)$. Then the efficiency of solution technique is determined by

the formula $\Delta_2 = \frac{H(P_1) - H(P_2)}{\Delta_1}$ with the assumption

that $L(P_1) \le H(P_2) \le H(P_1)$. The closer Δ_2 to the unit, the higher is the effect from simulating at the dynamic graph. The calculations showed that $\Delta_2 \approx 0,2$, i. e. simulating on the dynamic graph, allows reducing delivery time or both indices approximately by 20 %. Besides, the parameter depends significantly on the degree and structure of graph loading, amount and spread of clients.

Conclusion

The model of urban road system simulating complex characteristics, changing within the time and inherent to real road networks of modern cities has been created. The technique of routes searching of service traffic movement taking into account the peculiarities of real road network was realized on the basis of genetic search architecture. The software product representing the system of vehicles routing was developed. The system collects, stores and prepares information about clients, current orders, URS state, available vehicles as well as direct VRP solution by one of realized technique.

- 4. Kristofides N. Graph theory. Algorithm approach. Moscow: Mir, 1978.
- Emelyanov V.V., Kureichik V.M., Kureichik V.V. Theory and practice of evolutionary modeling. Moscow: Phismatlit, 2003.
- 6. Materials of the site http://qai.narod.ru/GA/index.htm
- 7. Materials of the site www.citforum.ru
- Materials of the site http://neo.lcc.uma.es/radiaeb/WebVRP//main.html

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